

ITEC451
Activity 17 - Solutions

Let $x_i = 1$ if server i is included in the initial set.

$x_i = 0$ otherwise

Then appropriate IP is

$$\begin{aligned} \max z &= 3x_1 + 2x_2 + 2x_3 + x_4 + 3x_5 + 3x_6 + x_7 \\ \text{s.t. } &x_1 + x_3 + x_5 + x_7 \geq 4 \text{ (service 1)} \\ &x_3 + x_4 + x_5 + x_6 + x_7 \geq 2 \text{ (service 2)} \\ &x_2 + x_4 + x_6 \geq 1 \text{ (service 3)} \\ &x_1 + x_2 + x_3 + x_4 + x_5 + x_6 + x_7 = 5 \text{ (five servers in the initial set)} \\ &3x_1 + 2x_2 + 2x_3 + x_4 + 3x_5 + 3x_6 + 3x_7 \geq 10 \text{ (CPU power)} \\ &3x_1 + x_2 + 3x_3 + 3x_4 + 3x_5 + x_6 + 2x_7 \geq 10 \text{ (Memory)} \\ &x_1 + 3x_2 + 2x_3 + 3x_4 + 3x_5 + 2x_6 + 2x_7 \geq 10 \text{ (Number of users)} \\ &x_6 + x_3 \leq 1 \\ &-x_4 - x_5 + 2 \leq 2y \quad (\text{If } x_2 > 0 \text{ then } x_4 + x_5 \geq 2) \\ &x_2 \leq 2(1-y) \\ &x_2 + x_3 \geq 1 \\ &x_1, x_2, \dots, x_7, y \text{ are all 0-1 variables} \end{aligned}$$